

Some useful constants and formulae

Speed of light	$c = 2.9979 \times 10^8 \text{ m/s}$	Gravitational constant	$G = 6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2$
Permittivity constant	$\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$	Permeability constant	$\mu_0 = 1.26 \times 10^{-6} \text{ H/m}$
Near point $P_N = 25 \text{ cm}$		Planck's constant	$h = 6.63 \times 10^{-34} \text{ J} \cdot \text{s} = 4.14 \times 10^{-15} \text{ eV} \cdot \text{s}$
$e = 1.60 \times 10^{-19} \text{ C}$		atomic mass $m(^1\text{H}) = 1.007825 \text{ u}$	
$m_e = 9.11 \times 10^{-31} \text{ kg} = 0.000549 \text{ u}$		$1 \text{ u} = 1.6605 \times 10^{-27} \text{ kg} = 931.5 \text{ MeV}/c^2$	
$m_p = 1.6726 \times 10^{-27} \text{ kg} = 1.00728 \text{ u}$		$1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$	
$m_N = 1.6749 \times 10^{-27} \text{ kg} = 1.008665 \text{ u}$		$hc = 1240 \text{ eV} \cdot \text{nm}$	

Transverse Waves:

$$y(x, t) = y_m \sin(kx - \omega t) \quad k = \frac{2\pi}{\lambda} \quad \omega = \frac{2\pi}{T} = 2\pi f \quad v = \frac{\lambda}{T} = \lambda f = \frac{\omega}{k}$$

Electromagnetic Waves:

$$E(x, t) = E_m \sin(kx - \omega t) \quad B(x, t) = B_m \sin(kx - \omega t) \quad \frac{E_m}{B_m} = c$$

$$E_{rms} = \frac{E_m}{\sqrt{2}} \quad c = \frac{1}{\sqrt{\epsilon_0 \mu_0}} \quad \vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$$

$$S = \frac{1}{\mu_0} EB = \frac{1}{c\mu_0} E^2 \quad I = \frac{1}{c\mu_0} E_{rms}^2 \quad I = \frac{P_{source}}{4\pi r^2}$$

Unpolarized Light: $I = \frac{1}{2} I_0$

Fully Polarized Light: $I = I_0 \cos^2 \theta$

Law of reflection $\theta_1' = \theta_1$

Snell's Law $n_1 \sin \theta_1 = n_2 \sin \theta_2$

Total internal reflection $\theta_c = \sin^{-1} \frac{n_2}{n_1}$

Brewster angle $\theta_B = \tan^{-1} \frac{n_2}{n_1}$

Total Absorption $p_c = \frac{I}{c}$

Total Reflection $p_r = \frac{2I}{c}$

Mirrors and Lenses:

Spherical Mirrors/Thin Lenses: $\frac{1}{p} + \frac{1}{i} = \frac{1}{f} \quad m = -\frac{i}{p}$

Spherical Mirrors: $f = \frac{r}{2}$

Refracting Surface: $\frac{n_1}{p} + \frac{n_2}{i} = \frac{n_2 - n_1}{r} \quad i = -\frac{n_2}{n_1} p$

$$n = \frac{c}{v} \quad \lambda_n = \frac{\lambda}{n} \quad \Delta\phi = \frac{2\pi L}{\lambda} (n_2 - n_1) \quad \Delta\phi = \frac{2\pi\Delta L}{\lambda}$$

magnifier $m_\theta = P_N/f$

microscope $m = -[l P_N]/f_{obj} f_{ey}$

telescope $m = -f_{ob}/f_{ey}$

Constructive Interference: $\Delta L = d \sin \theta = m\lambda \quad , \quad m = 0, 1, 2, \dots$

Destructive Interference: $\Delta L = d \sin \theta = \left(m + \frac{1}{2}\right) \lambda$ $m = 0, 1, 2, \dots$

Intensity in double-slit interference $I = 4I_0 \cos^2 \frac{\phi}{2}$ $\phi = \frac{2\pi d}{\lambda} \sin \theta$

Interference from thin films: Maxima: $2L = \left(m + \frac{1}{2}\right) \frac{\lambda}{n_2}$ **Minima:** $2L = m \frac{\lambda}{n_2}$

Single-slit Diffraction:

Minima $a \sin \theta = m\lambda$ **Intensity** $I(\theta) = I_m \left(\frac{\sin \alpha}{\alpha}\right)^2$, where $\alpha = \frac{\phi}{2} = \frac{\pi a}{\lambda} \sin \theta$

Resolvability:

Resolving angle $\theta = 1.22\lambda/a$ circular aperture $\theta = 1.22\lambda/D$

Resolving power $RP = \theta L$

Resolving power for microscope (telescope) $RP = 1.22 \lambda f/D$

Double-slit Diffraction:

$I(\theta) = I_m (\cos^2 \beta) \left(\frac{\sin \alpha}{\alpha}\right)^2$, where $\alpha = \frac{\pi a}{\lambda} \sin \theta$ and $\beta = \frac{\pi d}{\lambda} \sin \theta$ **Maxima lines** $d \sin \theta = m\lambda$

Diffraction gratings:

Half-width of line $\Delta\theta_{hw} = \frac{\lambda}{Nd \cos \theta}$

Photon Energy $E = hf$ **Photoelectric effect** $hf = W + KE$ **Photon Momentum** $p = \frac{hf}{c} = \frac{h}{\lambda}$

Wien's law $\lambda_p \cdot T = 2.90 \times 10^{-3} \text{ mK}$

Compton scattering $\lambda' = \lambda + (h/mc)(1 - \cos \Phi)$

de Broglie Wavelength $\lambda = h/p$, $f = \frac{E}{h}$

Time-independent Schrödinger Equation $\frac{d^2\psi(x)}{dx^2} + \frac{8\pi^2m}{h^2}[E - U(x)]\psi(x) = 0$

$\Delta x \cdot \Delta p_x \geq h/2\pi$

Heisenberg Uncertainty Principle $\Delta y \cdot \Delta p_y \geq h/2\pi$ $\Delta E \Delta t \geq \hbar$

$\Delta z \cdot \Delta p_z \geq h/2\pi$

Wave function in 1-D Infinite Well

$\psi_x(x) = A \sin\left(\frac{n\pi}{L}x\right)$

Energy Level In 1-d Infinite Well

$E_n = \left(\frac{h^2}{8mL^2}\right)n^2$

Probability $\psi(x)^2$

Barrier tunneling $T = e^{-2kL}$ $k = \sqrt{\frac{2m}{\hbar^2}(E_{pot} - E)}$

Binding Energy:

$$\Delta E_{be} = \sum (mc^2) - Mc^2$$

Disintegration Energy:

$$Q = (\sum M_p c^2 - \sum M_d c^2)$$

Energy Levels for H-Atom **Probability of an electron in an H-atom, in the ground state, being found inside a sphere of radius r.**

$$E_n = -\frac{13.6eV}{n^2}$$

$$p(r) = 1 - e^{-2x}(1 + 2x + 2x^2), \text{ where } x = r/a$$

Magnetic Dipole Moment $\vec{\mu}_{orb} = -\frac{e}{2m} \vec{L}$ **where** $L = \frac{h}{2\pi} \sqrt{l(l+1)}$

z-component of angular momentum $L_z = m_l \frac{h}{2\pi}$ **Spin Angular Momentum** $S = \frac{h}{2\pi} \sqrt{s(s+1)}$

Radius of atomic nucleus $r = r_0 A^{1/3}$, where $r_0 = 1.2 \text{ fm}$

Radioactive Decay $N = N_0 e^{-\lambda t}$ **Decay Rate** $\Delta N/\Delta t = (N_0/\Delta t) e^{-\lambda t}$ **Half-life** $T_{1/2} = \frac{\ln 2}{\lambda} = \tau \ln 2$