

A 12-kg collar A is at rest in the position shown, but is then subjected to a tangential force $F = 24 + 12x^2$ (N). The kinetic coefficient of friction between the collar and rod, $\mu_k = 0.3$. Assume that the rod is smooth after the 2 m distance as it enters the circular portion and determine a) the velocity of the collar after it has traveled 2 meters, and b) the maximum height h the collar will reach.

The force F stops at point 2

$$\sum F_x = F - .3N = ma$$

$$= 24 + 12x^2 - .3(12)(9.81)$$

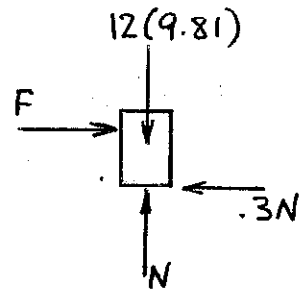
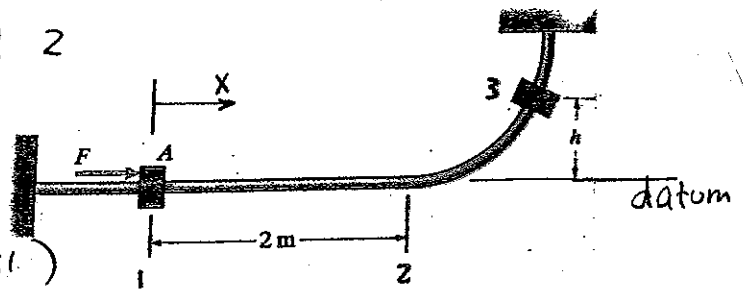
$$= 12v \frac{dv}{dx}$$

$$\int_0^2 (-11.316 + 12x^2) dx = 12 \int_0^v v dv$$

$$-11.316(2) + 12 \frac{(2)^3}{3} = 12 \frac{v^2}{2}$$

$$v = 1.25 \text{ m/sec}$$

$$v^2 = 1.561 \text{ m}^2/\text{sec}^2$$



$$T_2 + V_2 + U_{1-2} = T_3 + V_3$$

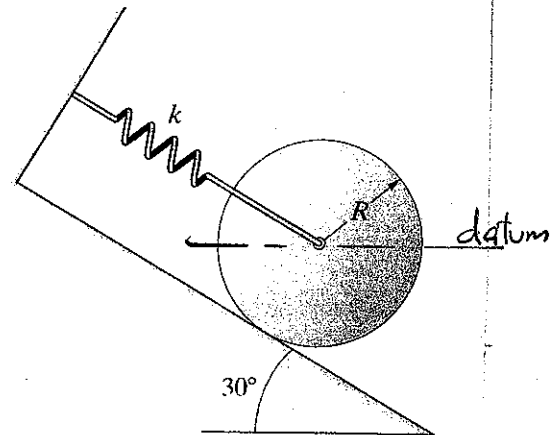
$$\frac{1}{2}(12)(1.561) + 0 + 0 = 0 + 12(9.81)h$$

$$h = 0.0795 \text{ m}$$

The disk shown weighs 12 lbs and its radius $R = 6$ in. The spring constant $k = 3$ lb/ft. The disk is released from rest with the spring unstretched and rolls without slipping. Determine the magnitude of the velocity of the center of the disk when it has moved 2 ft from its original position.

Using energy method

$$\begin{aligned}
 T &= \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 \\
 &= \frac{1}{2}mv^2 + \frac{1}{2}\left[\frac{1}{2}mR^2\right]\left(\frac{v}{R}\right)^2 \\
 &= \frac{3}{4}mv^2
 \end{aligned}$$



$$T_1 + V_1 + U_{1-2} = T_2 + V_2$$

$$0 + 0 + 0 = \frac{3}{4}mv^2 + \frac{1}{2}kx^2 - mg \sin 30^\circ(2)$$

$$0 = \frac{3}{4}\left(\frac{12}{32.17}\right)v^2 + \frac{1}{2}(3)(2)^2 - 12(.5)(2)$$

$$v^2 = 21.44$$

$$v = 4.63 \text{ ft/sec} \rightarrow$$

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$$\begin{aligned} \sum F_x &= -F - kx + mg \sin \theta = ma \\ &= -F - 3x + 12 \sin 30^\circ = \frac{12}{32.17} a \end{aligned}$$

$$\begin{aligned} \sum F_y &= N - mg \cos \theta = 0 \\ N &= 12 \cos 30^\circ = 10.39 \text{ lb} \end{aligned}$$

$$\sum M_c = F \left(\frac{12}{32.17} \right) = I \alpha = \frac{1}{2} m R^2 \left(\frac{a}{R} \right)$$

$$F = \frac{1}{2} \left(\frac{12}{32.17} \right) a = .1865 a$$

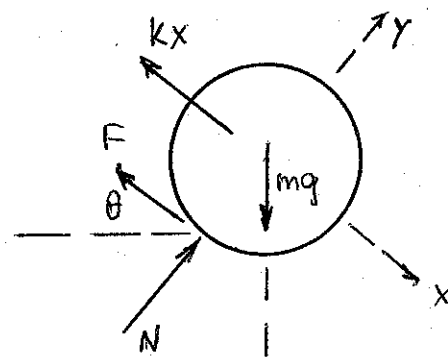
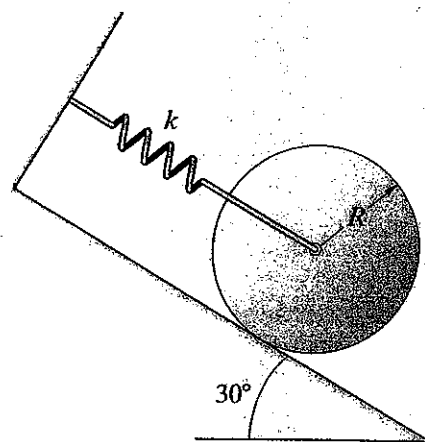
$$-.1865 a - 3x + 6 = .373 a$$

$$-3x + 6 = .559 v \frac{dv}{dx}$$

$$-3 \int_0^2 x dx + 6 \int_0^2 dx = .559 \int_0^v v dv$$

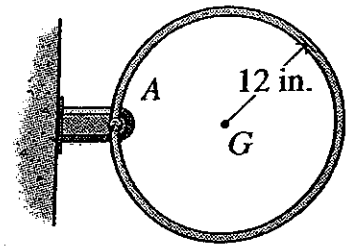
$$-\frac{3(2^2)}{2} + 6(2) = .559 \frac{v^2}{2}$$

$$v = 4.63 \text{ ft/sec}$$



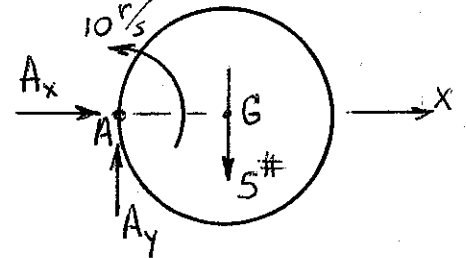
A thin ring, 24 inches in diameter, weighs 5 lbs and rotates in a vertical plane about a point A with an angular velocity of 10 rad/sec counterclockwise. For the position shown, determine a) the angular acceleration α of the ring about A, and b) the x and y components of the force at A.

For the ring $I_A = mr^2 + mr^2 = 2mr^2$
 $= \frac{5}{32.17} (2)(1)^2$
 $= 0.3108 \text{ slug ft}^2$



$$+\sum F_x = A_x = \frac{5}{32.17} a_{Gx} = \frac{5}{32.17} \left(-\frac{12}{12}\right) 10^2$$

$$A_x = 15.54 \text{ lb}$$

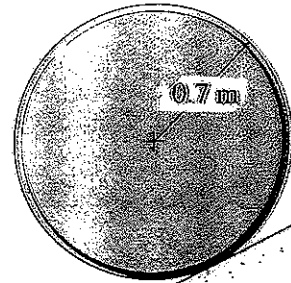


$$+\sum F_y = -A_y + 5 = \frac{5}{32.17} \left(\frac{12}{12}\right) \alpha = .155 \alpha$$

$$\left(+\sum M_A = \left(\frac{12}{12}\right) 5 = .3108 \alpha \quad \alpha = 16.08 \text{ r/s}^2\right)$$

$$A_y = 5 - .155(16.08) = 2.50 \text{ lb}$$

A 45-kg cylinder is placed on a 25° inclined surface from rest as shown. The diameter of the cylinder is 1.4 m. The cylinder rolls without slipping. Use the energy method to determine a) the angular velocity, ω and b) the angular acceleration, α of the cylinder after it has rolled 10 meters down the incline.



$$T_1 + V_1 + U_{1-2} = T_2 + V_2$$

$$0 + 0 + 0 = \frac{3}{4} (45) v_2^2$$

$$- (45)(9.81)(10) \sin 25^\circ$$

$$v = 7.43 \text{ m/s}$$

$$\omega = \frac{v}{r} = \frac{7.43}{.7} = \underline{10.62 \text{ rad/sec}}$$

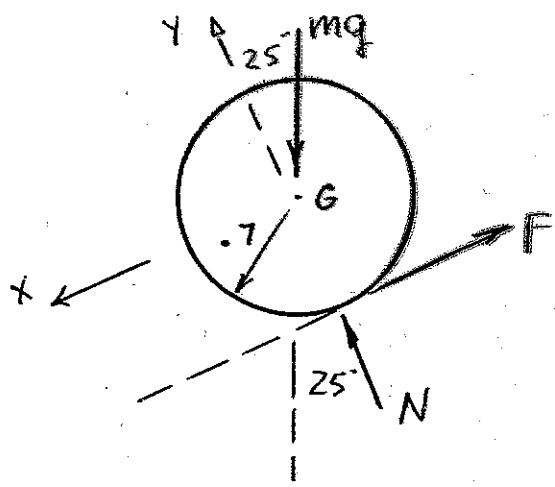
$$\begin{aligned} \sum F_x &= (45)(9.81) \sin 25^\circ - F \\ &= (45) a = 45 (.7) \alpha \end{aligned}$$

$$\text{or } F = 186.56 - 31.5 \alpha$$

$$\sum M_G = .7 F = I \alpha = \frac{1}{2} (45) (.7)^2 \alpha$$

$$\text{or } F = 15.75 \alpha$$

$$\alpha = \underline{3.95 \text{ rad/sec}^2}$$



Confirmation:

$$\alpha = \omega \frac{d\omega}{d\theta} \quad \int_0^\theta \alpha d\theta = \int_0^\omega \omega d\omega$$

$$2\alpha\theta = \omega^2 \quad \theta = \frac{10}{.7} = 14.286 \text{ rad}$$

$$\omega^2 = 2(3.95)(14.286)$$

$$\omega = \underline{10.62 \text{ rad/sec}}$$

A 24-in diameter disk weighs 130 lbs and has a radius of gyration about point A of $k_A = 9$ inches. A cord wrapped around the periphery of the disk passes over a small pulley of negligible mass and is attached to a 70-lb block B. The system is released from rest. Determine a) the tension in the cord, and b) the acceleration of the block as the motion begins.

$$\begin{aligned} \left(+ \sum M_A \right) &= \frac{12}{12} T - \frac{5}{12} (130) \\ &= I_A \alpha = 2.27 \alpha \end{aligned}$$

$$T = 54.17 + 2.273 \alpha$$

$$a_B = \frac{12}{12} \alpha$$

$$\left(+ \sum F_B \right) = 70 - T = \frac{70}{32.17} a_B$$

$$T = 70 - 2.176 \alpha = 54.17 + 2.273 \alpha$$

$$\alpha = 3.558 \text{ r/s}^2$$

$$a_B = 3.558 \text{ ft/sec}^2$$

$$T = 62.25 \text{ #}$$

