

## Chapter 5: First Law of Thermodynamics: Closed Systems

**Work:** Work is a force acting through a distance,  $\dot{W}$   
Power is work per unit time,

$$\text{Boundary Work} \quad W_b = \int F ds = \int P A ds = \int P dV$$

$$\text{Electrical Work} \quad W_e = V N \text{ (kJ)} \quad W_e = V I \quad \text{(kW)}$$

$$\text{Work of a Spring} \quad W_{\text{spring}} = \frac{1}{2} k_s (x_2^2 - x_1^2) \quad \text{(kJ)}$$

### First Law of Thermodynamics:

$$Q - W = \Delta E \quad \Delta E = \Delta U \text{ for closed systems}$$

$$\text{Specific Heats:} \quad C_v = \left( \frac{\partial u}{\partial T} \right)_v \quad C_p = \left( \frac{\partial h}{\partial T} \right)_p$$

### Internal Energy, Enthalpy and Specific Heats of an Ideal Gas:

$$\Delta u = c_v \Delta T \quad \Delta h = c_p \Delta T \quad P v = R T$$

$$dh = du + R dT \quad C_p - C_v = R \quad k = C_p / C_v$$

### Internal Energy, Enthalpy and Specific Heats of Solids and Liquids:

$$C_p = C_v = C \quad \Delta u = C \Delta T \quad \Delta h = \Delta u + v \Delta P$$

## Thermodynamics Processes for Closed Systems:

- Constant Volume Process: ( $V = C$ )

$$W_b = \int P dV = 0$$

- Constant Pressure Process: ( $P = C$ )

$$W_b = \int P dV = P(V_2 - V_1)$$

- Constant Temperature Process of an Ideal Gas: ( $T = C$ )

$$\begin{aligned} W_b = \int P dV &= \int \frac{mRT}{V} dV = mRT \ln \frac{V_2}{V_1} = P_1 V_1 \ln \frac{V_2}{V_1} \\ &= P_1 V_1 \ln \frac{P_1}{P_2} \end{aligned}$$

- Polytropic Process: ( $P V^n = C$ )

$$W_b = \int P dV = \frac{P_2 V_2 - P_1 V_1}{1 - n} \quad n \neq 1$$

- Isentropic Process: ( $P V^k = C$ )  $k = \frac{c_p}{c_v}$   
 $1.0 < k \leq 1.67$

For Monatomic Molecules (He, Ar, Kr, Ne, Xe)  $k = 1.67$

For Diatomic Molecules ( $N_2$ ,  $O_2$ ,  $CO_2$ , CO, Air)  $k = 1.40$

For More Complicated Molecules ( $CH_4$ ,  $NH_3$ , etc.)  $k = 1.33$

For gases at high temperatures  $1.15 \leq k \leq 1.30$